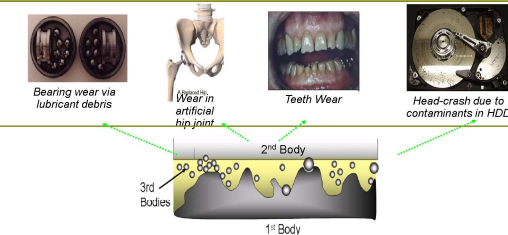


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Computational Modeling Approach: PAML



Particle Augmented Mixed Lubrication → Applied load is carried by both fluid pressure and contact stress, in presence of particles

```

graph TD
    Root[ ] --- FM[Fluid Mechanics]
    Root --- CM[Contact Mechanics]
    Root --- PD[Particle Dynamics]
    Root --- W[Wear]
    FM --- FT[Film thickness  
h = h(θ, ϕ)]
    CM --- SC[Separation  
ΔH = ΔH(θ, ϕ)]
    PD --- PG[Particle generation  
Uniform distribution  
from debris]
    W --- MR[Material Removal  
Volume(θ, ϕ) = K_wear * (F * V_solid(θ, ϕ)) / H_wear]
    FT --- HD[Hydrodynamic Pressure  
p = p(h, η, ω)]
    SC --- EC[Elastic Contact  
σ(θ, ϕ) = (E(1-ν) / (1-2ν)(1+ν)Γ) * ΔH(θ, ϕ)]
    PG --- PT[Particle transport  
Uniform Concentration]
    EC --- EQ[Equilibrium]
    PT --- PD2[Particle deposition  
Volume=f(G, v, D)]
  
```

The flowchart illustrates the relationships between four main sub-disciplines of tribology: Fluid Mechanics, Contact Mechanics, Particle Dynamics, and Wear. Each sub-discipline has associated parameters and equations, and they are interconnected through various physical processes.

- Fluid Mechanics** leads to **Film thickness** ($h = h(\theta, \phi)$), which then leads to **Hydrodynamic Pressure** ($p = p(h, \eta, \omega)$), and finally to **Equilibrium**.
- Contact Mechanics** leads to **Separation** ($\Delta H = \Delta H(\theta, \phi)$), which then leads to **Elastic Contact** ($\sigma(\theta, \phi) = \frac{E(1-\nu)}{(1-2\nu)(1+\nu)\Gamma} \Delta H(\theta, \phi)$), and finally to **Equilibrium**.
- Particle Dynamics** leads to **Particle generation** (Uniform distribution from debris), which then leads to **Particle transport** (Uniform Concentration), and finally to **Particle deposition** (Volume=f(G, v, D)).
- Wear** leads to **Material Removal** ($\text{Volume}(\theta, \phi) = K_{\text{wear}} \frac{(F \cdot V_{\text{solid}}(\theta, \phi))}{H_{\text{wear}}}$).

UHMWPE or Metallic Acetabular Liner

Ceramic or Metallic Femoral Head

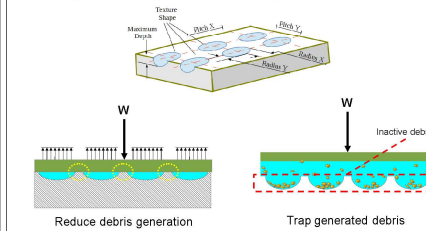
Newtonian Synovial Fluid Lubrication

SIMULATED SETUP

Conclusions

Figure 10 consists of four 3D surface plots arranged in a 2x2 grid. The top row shows results for the femoral head, and the bottom row shows results for the acetabular cup. The left column displays fluid pressure, and the right column displays wear. Each plot includes a color scale bar on the right side. The pressure plots have a scale from 0 to 10,000 Psi, with colors ranging from blue (low) to red (high). The wear plots have a scale from 0 to 0.0001 mm³/mm², with colors ranging from blue (low) to red (high). A black arrow in each plot points to a specific location on the surface. The femoral head plots show a spherical shape with a central indentation, while the acetabular cup plots show a cup-like shape with a central protrusion.

- High-fidelity deterministic modeling is critical to fully leverage patient-specific prosthesis design



Pitch Ratio (Pitch / Texture Surface Radius)	Material Removed (μm)
Pitch 2.0	~2405.5
Pitch 2.5	~2403.5
Pitch 3.0	~2404.5
Pitch 3.5	~2404.5

Total material removed from the surface of the cup

Pitch Ratio (Pitch / Texture Surface Radius)	Material Deposited (µm)
Untextured	0
Pitch 2.0	45
Pitch 2.5	30
Pitch 3.0	18
Pitch 3.5	13

Total material trapped in the textures

Pitch Ratio (Pitch/Texture Surface Radius)	Concentration in [0-1] (value %2)
Untextured	0.68
Pitch 2.0	0.02
Pitch 2.5	0.45
Pitch 3.0	0.62
Pitch 3.5	0.65

1. Jhurani, S. M., and Higgs, C. F., "An elastohydrodynamic lubrication (EHL) model of wear particle migration in an artificial hip joint," *Tribology International*, 43 (8), 1326-1338, Aug. 2010.
2. Wang, F. and Jin, Z. "Lubrication modelling of artificial hip joints: From fluid film to boundary lubrication regimes", 2004, *American Society of Mechanical Engineers*, New York, NY 10016-5990
3. Ito, H., Kaneda, K., Yuhita, T., Nishimura, I., Yasuda, K., Matsuno T., "Reduction of polyethylene wear by concave dimples on the frictional surface in artificial hip joints," *J Arthroplasty*, 15(3): 332-8, Apr. 2000
4. Gao, L., Yang, P., Dymond, I., Fisher, J., and Jin, Z., "Effect of surface texturing on the elastohydrodynamic lubrication analysis of metal-on-metal hip implants," *Tribology International*, vol. 43, no. 10, pp. 1851-1869, Oct. 2010.

- ICES-Dowd Fellowship